Elliptic subcovers of a genus two curve

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Abstract

Let C be a curve of genus 2 and let E be an elliptic curve such that there is a map $\phi: C \longrightarrow E$ of degree n. Then this induces a map $\psi: \mathbb{P}^1 \longrightarrow \mathbb{P}^1$. Under certain conditions, there exists an elliptic curve E' such that the jacobian of C is isogenus to the product $E \times E'$. We will discuss an algorithm for finding an appropriate curve, E', for the cases of small odd degree.