Extreme eigenvalues of non-regular graphs

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Abstract

Let λ_1 be the greatest eigenvalue and λ_n the least eigenvalue of the adjacency matrix of a connected graph G with n vertices, m edges and diameter D. We prove that if G is nonregular, then

$$\Delta - \lambda_1 > \frac{n\Delta - 2m}{n(D(n\Delta - 2m) + 1)} \ge \frac{1}{n(D+1)}$$

where Δ is the maximum degree of G.

The inequality improves previous bounds of Stefanović and of Zhang. It also implies that a lower bound on λ_n obtained by Alon and Sudakov for (possibly regular) connected nonbipartite graphs also holds for connected nonregular graphs. This is joint work with David Gregory and Vlado Nikiforov.