

# Some Recent Advances & Open Problems on Perturbations and Extensions of Isometric Operators

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In this talk, some recent advances & open problems on perturbations and extensions of isometric operators are presented. For example, on the "strong-stability problem for the linear isometries" we obtain some positive results on the spaces  $B(E_2, L(m))$ ,  $B(E_n, C(K))$ ,  $B(L^{(\infty)}, (m))$  and  $B(X, L^{(\infty)})$  (where  $X$  is uniformly smooth with  $\dim X = 1$  or  $\infty$ ) but what about for the space  $B(L^{(p)}, C(K))$ ? And on the "extension problem of isometry between the unit spheres of two Banach spaces" we obtain some positive results on the spaces  $B(H)$ ,  $B(l^{(p)})$  and  $B(E, C(K))$  but what about for the isometry which is defined the sphere of  $E$  "into" (not "onto") the sphere of  $F$ ? etc.