## PIMS Elementary Grades Math Competition 29 May 2004

NAME:

Sprint Round - Grade Six Division

SCHOOL:

1. Find:  $1+2+4+8+\cdots+512 =$ 

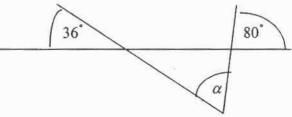


2. Find:  $\frac{\frac{13}{33} - \frac{1}{11}}{\frac{16}{33}} \times \frac{16}{23} =$ 



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3. Find the angle  $\alpha$ .



- 4. What is the remainder when  $1 \times 2 \times 3 \times \cdots \times 10 \times 11 + 3^2$  is divided by 7?
- 5. What is the product of all the prime factors of 120?
- 6. Find the value of:  $(77 \times 7) + (11 \times 7) + (22 \times 7) =$  \_\_\_\_\_6
- 7. Three workers need 15 hours to finish a job. How many hours are needed for five workers to finish the same job if they work at the same speed?
  7
- 8.  $\frac{x}{y} = 2.5$  and  $\frac{x+y}{x-y} = 2\frac{8}{z}$ . What is the value of z?
- 9. On a planet far away, the year is 600 days long, and weeks are still 7 days long with the same names for each day of the week as on planet Earth. On one year, New Year's day was on Sunday. On what day of the week was the next New Year's day?
- 10. What is  $\frac{a}{b} \times (a \times b) \times \frac{9}{b}$  when a = 7 and b = 3?
- 11. There are eleven teams in a basketball tournament. Each team must play all other teams exactly twice. How many games need to be played in this tournament? \_\_\_\_\_\_11
- 12. Joe runs at a rate of 5 meters/sec. Jane runs at a rate of 8 meters/sec.

  If Joe and Jane have a race and Jane starts 160 meters from the finish line, how far ahead of Jane should Joe start (in meters) so they both reach the finish line at the same time?
- 13. Calculate: 19 + 78 + 80 + 21 + 82 + 17 = \_\_\_\_\_\_13

14. The base of a pyramid has 6 sides. How many vertices does the pyramid have? 14 15. A number N has the form 323232...32 and is divisible by 9. What is the smallest number of digits that N can have? 15 16. What is the sum of the first 2004 terms of the sequence 0,1,2,0,1,2,0,1,2,...? 16 17. a, b, and c, the lengths of the sides of the triangle ABC, are whole numbers. We know that a = 7 and that b = 11. What is the minimum possible value of c?  $\sqrt{17^2 - 15^2} - (\sqrt{17^2} - \sqrt{15^2}) =$ 18 18. Find the value of the expression: 19. There are 31 students in a classroom. Of these students, 16 are girls. 7 of the students have pierced ears. If 12 of the boys do not have pierced ears, how many of the girls have pierced ears? 19 20. The circumference of a circle and the perimeter of a pentagon can 20 intersect at a maximum of N points. What is N? 21. What is the smallest even whole number the sum of whose decimal digits is 33? 21 22. A pot full of water weighs 2 kg (the total combined weight of the pot and the water). If we spill out 20% of the water, the weight of the pot and the water together is 88% of the original weight. What is the weight of the empty pot in kg? (Give your answer as a decimal expression). 22 23. A farmer has only chickens and cows. If you count the legs of the chickens (two legs each) and the legs of the cows (four legs each), there are a total of 720 legs altogether. Also, there are 4 times as many cows as there are 23 chickens. How many cows are there on the farm? Define a new operation "&". For X, Y any two numbers,  $X \& Y = \frac{X}{Y + Y}$ . 24. Suppose that  $X \& Y = \frac{1}{3}$ . Find the value of Y & X. 24 25. Sheila can fill her backpack, without leaving any wasted space, with (a) 4 video cassettes and 21 DVDs, or (b) 3 binders and 4 video cassettes, or (c) 5 binders. If she fills her backpack with DVDs only, how many DVDs can she fit in her backpack? 25